

Chemically Accurate Relative Folding Stability of RNA Hairpins from Molecular Simulations

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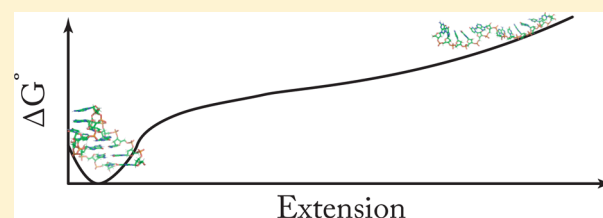
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S Supporting Information

ABSTRACT: To benchmark RNA force fields, we compared the folding stabilities of three 12-nucleotide hairpin stem loops estimated by simulation to stabilities determined by experiment. We used umbrella sampling and a reaction coordinate of end-to-end (5' to 3' hydroxyl oxygen) distance to estimate the free energy change of the transition from the native conformation to a fully extended conformation with no hydrogen bonds between non-neighboring bases. Each simulation was performed four times using the AMBER FF99+bsc0+ χ_{OL3} force field, and each window, spaced at 1 Å intervals, was sampled for 1 μ s, for a total of 552 μ s of simulation. We compared differences in the simulated free energy changes to analogous differences in free energies from optical melting experiments using thermodynamic cycles where the free energy change between stretched and random coil sequences is assumed to be sequence-independent. The differences between experimental and simulated $\Delta\Delta G^\circ$ are, on average, 0.98 ± 0.66 kcal/mol, which is chemically accurate and suggests that analogous simulations could be used predictively. We also report a novel method to identify where replica free energies diverge along a reaction coordinate, thus indicating where additional sampling would most improve convergence. We conclude by discussing methods to more economically perform these simulations.



INTRODUCTION

RNA is central to life.¹ It has fundamental roles in the expression of genetic information as proteins and also functions directly in other processes as noncoding RNA.^{2–14} Molecular interactions are the first principles of biology in that they allow mechanistic understandings of biology. Hence, all-atom simulations of RNA provide a framework for developing hypotheses and interpreting experiments.^{15–19}

Molecular dynamics (MD) uses classical mechanics to model the motions of molecules. Snapshots of the simulated system recorded periodically during the simulation approximate the thermodynamic conformational ensemble that, with thorough sampling, can be compared to experimental measurements. Making this comparison, however, requires knowing the relationship between the coordinates in the snapshots and the experimental quantity measured.^{20–26}

MD simulations require an energy model known as a force field, which estimates the potential energy from the molecular conformation. The force field functional form and parameters are approximations of the quantum mechanics of the electronic structure underlying the molecular interactions.^{20,27,28} There are a number of known limitations to the RNA force fields that lead to significant artifacts in the simulations when sampling is thorough. In simulations with the commonly used AMBER force field, FF99+bsc0+ χ_{OL3} ,^{29–31} tetraloops do not retain a folded

structure,^{32,33} tetramers often lack contacts observed in proton NMR spectra and exhibit close contacts not observed in the spectra,^{25,32} internal loops do not produce ratios of major and minor conformers similar to solution structures,^{34,35} and some RNA–protein complexes are not stable for more than 1 μ s.³⁶ It is widely believed that no available force field cheap enough to permit adequate sampling is accurate enough to fold structured RNA de novo.^{27,28,37} The CHARMM 36 force field³⁸ and a revised Amber force field³⁹ neither correctly stabilize the native tetraloop structure nor accurately model tetramers.³² Our recent work reparameterizing backbone dihedrals improves simulation accuracy for tetramers and internal loops but not tetraloops.⁴⁰ Another revision of the AMBER force field and a new AMOEBA force field for nucleic acids were recently published but remain to be tested by the field more broadly.^{41,42} Here we provide a different framework for testing force fields and apply it to AMBER's FF99+bsc0+ χ_{OL3} force field.

One strategy for force field benchmarking is to compare thermodynamic quantities estimated by simulation to reference data. One such quantity with extensive reference data is the unfolding free energy change of small structured RNAs.^{34,43} Benchmarking against free energy changes tests whether the

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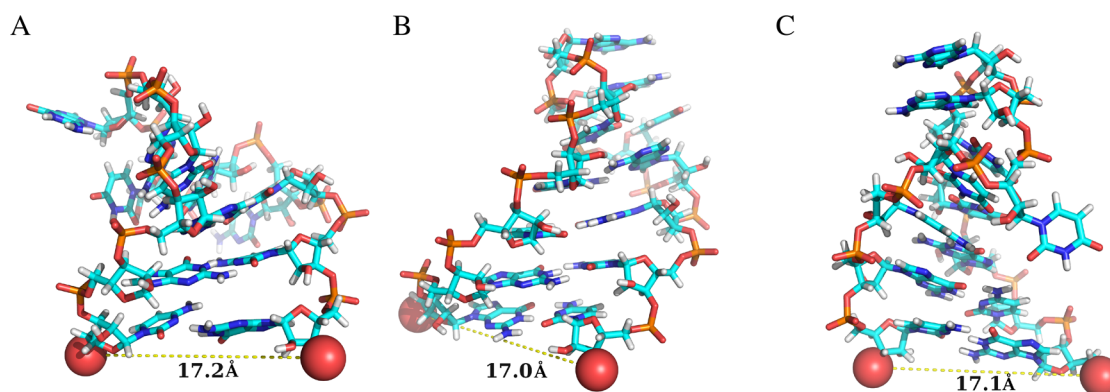


Figure 1. Starting structures for the pulling denaturation simulations. (A) Sequence 1, with loop sequence CAGUGC. (B) Sequence 2, with loop sequence GUAAUA. (C) Sequence 3, with loop sequence UUAAUU. Structures are shown as sticks with carbons in cyan, nitrogens in blue, hydrogens in white, oxygens in red, and phosphoruses in orange. The oxygens used to measure the end-to-end distance are shown as spheres, and their native distances are indicated with dashed lines and by the boldface number in Å.

simulated volume of the native conformational basin is accurate and whether the force field correctly represents the favorability of native contacts relative to those in the unfolded state. This contrasts to comparisons between simulations and native structures determined by NMR or crystallography, where it is difficult to assess whether the observed conformational flexibility is consistent with the structure unless the native conformation is catastrophically lost. Simulated free energy changes have been previously compared to in vitro reference data for base stacking stability,^{44–47} helix stability,^{48–51} and small hairpin stability.^{38,52–55}

This study compares the relative free energy changes of stretching RNA hairpin stem loops estimated by simulation to free energy changes determined by optical melting experiments using thermodynamic cycles.⁵³ Simulating the optical melting transition with good statistics is challenging because the denatured state has a huge volume in phase space.^{56,57} Thus, to focus our sampling, we simulate a transition along a distance from folded to stretched, in imitation of force denaturation by optical tweezers, hereafter referred to as pulling experiments.^{53,58,59}

To simulate this stretching transition, we performed umbrella sampling along the 5' to 3' hydroxyl oxygen distance (the end-to-end distance). We performed these simulations in quadruplicate for three 12-nucleotide RNAs with known free energies of unfolding and with representative NMR structures (Figure 1). We compared the simulated change in free energy of stretching to experimentally determined free energy changes of melting for pairs of sequences with thermodynamic cycles.⁵³ The mean absolute difference between the reference and simulated $\Delta\Delta G^\circ$ is 0.98 kcal/mol. Our analysis suggests that the residuals for each sequence, which on average have an error of 0.66 kcal/mol (approximately $k_B T$ at 37 °C), are accurate and precise enough to have a predictive value and set a new standard for precision in such simulations.

METHODS

Starting Structures. We used three hexamer RNA hairpin loops for which NMR structures and optical melting data were both available. For each NMR structure, we used the first conformer provided in the PDB. Below we provide the sequence, where underlining is used to indicate the residues in the loop, as well as references to the deposited coordinates and to the reported stability of each loop.

1. CGA CAGUGC UCG, corresponding to the loop structure with PDB ID of 1AQO (Figure 1A).⁶⁰ We excised the hairpin loop and closing base pair from the larger structure (CAA CAGUGC UUG, residues 10–21). To stabilize the stem, we changed the identity of the nucleotides in the closing helix to two GC pairs by manually changing atom types. This hexaloop caps the iron responsive element that regulates translation of iron associated transcripts by changing their availability to the translation machinery. The experimental free energy change of unfolding of the adjusted structure at 37 °C is -0.21 ± 0.39 kcal/mol.^{61–63}
2. GGC GUAAUA GCC. We used the first conformer from a solution NMR structure reported by Fountain et al. (Figure 1B).⁶⁴ The occurrences of this loop in rRNA tend to have a sugar–Hoogsteen GA pair between the first and last residues of the loop;⁶⁵ however, in the NMR structure, this noncanonical pair is only partially present.⁶⁴ The experimental free energy change of unfolding at 37 °C is -3.46 ± 0.24 kcal/mol.⁶⁶
3. GCG UUAAUU CGC, corresponding to the solution NMR structure deposited in the PDB as 1HS3 (Figure 1C).⁶⁷ The experimental free energy change of unfolding at 37 °C is -2.36 ± 0.32 kcal/mol.⁶⁸

We refer to these chemical systems by the sequence of their loops (for example, sequence 1 will be called CAGUGC).

There are two approaches to estimate experimental uncertainty in folding free energy from optical melting experiments:

1. the average uncertainties observed for the ΔH° (12%) and ΔS° (13.5%) for the database of melting experiments following eq 11 of Xia et al.,⁶⁹ which accounts for the correlation in ΔH° and ΔS° .^{63,69}
2. the uncertainty in the free energy change provided with the melt.

To be conservative, we calculated both uncertainties for each sequence and took whichever was greater. We used the statistical method for CAGUGC and UUAAUU, and the uncertainty provided with the melt for GUAAUA.

Sequence 1 was edited in the closing stem helix as compared to the sequence studied by NMR and optical melting experiments. Nearest-neighbor rules were used to estimate the free energy of unfolding for the revised sequence:⁶⁹ the nearest-

neighbor stacking terms for the removed base pairs were subtracted from the experimentally determined folding stability, and the stacking terms for the new base pairs were added. Because these modifications were made in an A-form helix, where the nearest-neighbor rules are most accurate, the estimated error from the nearest-neighbor parameter terms was 0.12 kcal/mol, which resulted in a 0.02 kcal/mol increase in the propagated error estimate of the optical melting experiment.⁶⁸ We used the error estimates, including parameter covariance, to estimate the overall error.⁷⁰

Simulation Protocol. We chose to monitor and bias folding along the distance between the 5' and 3' hydroxyl oxygens of the terminal residues of each 12-mer. This simulates the effect of applying force to the hairpin through tethers attached to its 5' and 3' ends, as has been done in single-molecule experiments using optical tweezers.⁵⁹ Here we simulated this transition with umbrella sampling, whereby the molecule was restrained to occupy specific positions along the reaction coordinate in independent equilibrium simulations called windows.^{27,71,72} The biased distributions of reaction coordinate positions were then unbiased to determine the free energy curve (FEC) using the weighted histogram analysis method (WHAM) to iteratively minimize the statistical errors in overlapping regions from each simulation.⁷³

Simulations were run using the GPU code⁷⁴ from the AMBER 14 and AMBER 16 packages.^{75,76} We simulated four replicas of each window for each molecule. Equilibrium distances were spaced in 1 Å increments from 15 to 60 Å, and a harmonic restraint with a force constant of 3 kcal mol⁻¹ Å⁻² was used to bias sampling at each distance. The native distance occupied by the NMR structures chosen was approximately 17 Å for each structure (Figure 1). The molecular coordinates of the 17 Å window were taken directly from the solution structures. Subsequent windows were generated by solvating the coordinates from the last frame of a 2 ns solvated MD simulation on the previous window. This procedure was repeated independently for each replicate, so that the starting structures were different.

Each window was built with truncated octahedral periodic boundary conditions with a 10 Å minimum distance between the solute and the periodic boundary. Each window was solvated with TIP3P water with neutralizing sodium and with an additional 1 M NaCl to simulate the conditions of the melting experiments. Each system was maintained at 310 K using Langevin dynamics with a time step of 2 fs and with bonds involving hydrogen constrained by SHAKE.^{77,78} The collision frequency of the thermostat was 2 ps⁻¹, and pressure was maintained using a Monte Carlo barostat with a 100 step attempt frequency. Each simulation was run for 1 μs. Because there were 46 windows per replica of each pulling simulation and there were four replicas per molecule, this amounts to 4 × 46 × 3 = 552 μs of aggregate simulation time.

Hydrogen Bond Averaging. To compute the average number of base–base hydrogen bonds we used cpptraj from the AmberTools Suite.⁷⁵ We then postprocessed the results using awk to exclude backbone and neighboring base interactions. We averaged this quantity across the four replicas for each window and computed the standard error of its mean (SEM).

Free Energy Analysis. For each window, the 3' to 5' distance was recorded every 10 000 steps (20 ps), leading to 200 000 sampled distances per trajectory. The first 200 ns of each simulation was discarded as equilibration. Umbrella sampling simulations were merged into one free energy curve

along the reaction coordinate for each system using WHAM^{73,79,80} with the following parameters: a minimum distance of 14.95 Å, a maximum distance of 60.05 Å, with 451 bins and a convergence criterion of 1.0 × 10⁻⁶ kcal/mol for maximum successive difference for the free energy change.⁸⁰ The reaction coordinate was broken into two states: slack and stretched divided at 45 Å. The slack state included the native-like windows near 17 Å. We chose the distance for this division of the two states based on the average number of non-neighboring base–base hydrogen bonds (see the section entitled [Hydrogen Bonding and Reaction Coordinate Partitioning](#) and Figure 4).

We defined the free energy change of stretching a sequence A as

$$\Delta G_{\text{stretch}}^{\circ}(A) = RT \ln \left(\frac{\sum_{i \geq c} P_i}{\sum_{i < c} P_i} \right) \quad (1)$$

where R is the gas constant, T is the temperature in Kelvin, i is the bin index, c is the bin index corresponding to the cutoff distance of 45 Å, and P_i is the probability of the i th bin for sequence A. To compare the free energy changes estimated from simulations to those measured by optical melting, we used thermodynamic cycles (Figure 2).⁵³ This is necessary because

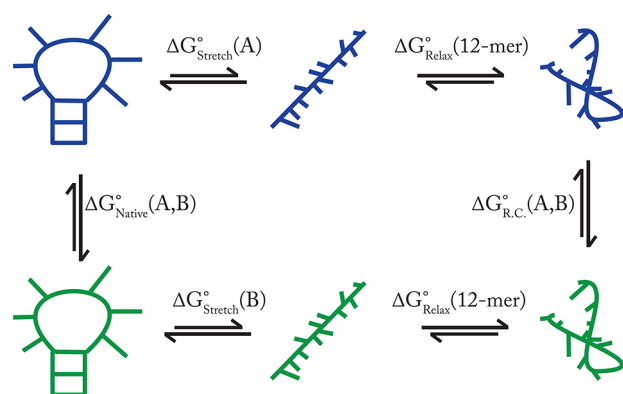


Figure 2. Thermodynamic cycle to compute $\Delta\Delta G_{\text{stretch}}^{\circ}(A,B)$ for sequences A and B. We simulate the transitions from native to stretched but not the transition from stretched to random coil, the end point of optical melting experiments. We can approximate these transitions as sequence-independent, here indicated by $\Delta G_{\text{Relax}}^{\circ}(12\text{-mer})$; thus, they cancel when $\Delta\Delta G^{\circ}$ are computed.⁵³ In the cycle, the free energies are subscripted to show in which conformational state the system ends, when read from right to left. The sequence or sequences involved in the transition is indicated in parentheses after the free energy; thus, alchemical transitions are given as involving two sequences. R.C. stands for random coil.

the denatured state is different for pulling than for thermal denaturation.^{53,59} For each pair of sequences (A and B), we subtracted the free energy differences from one another to compute

$$\Delta\Delta G_{\text{stretch}}^{\circ}(A, B) = \Delta G_{\text{stretch}}^{\circ}(A) - \Delta G_{\text{stretch}}^{\circ}(B) \quad (2)$$

We analogously define a difference in free energy of melting for sequences A and B (where the reference melt for sequence I is $\Delta G_{\text{ref}}^{\circ}(I)$)

$$\Delta\Delta G_{\text{melt}}^{\circ}(A, B) = \Delta G_{\text{ref}}^{\circ}(A) - \Delta G_{\text{ref}}^{\circ}(B) \quad (3)$$

We estimated error using the SEM of the four replicas.⁸¹ To compute the variance, the mean, μ , was the $\Delta G_{\text{pooled}}^{\circ}$ from applying WHAM to the pooled data from the four replicas. We

propagated errors using the customary formulas for the SEM as the best estimate of the uncertainty in a quantity q measured multiple times⁸¹

$$\text{SEM}(q) = \delta(q) = \frac{\sigma(q)}{\sqrt{N}} = \frac{1}{N} \cdot \sqrt{\sum_{i=1}^N (q_i - \mu)^2} \quad (4)$$

The uncertainty for quantity Q calculated by addition or subtraction of quantities, $\{k\}$, which have uncertainties, $\{\delta_k\}$, is

$$\delta(Q) = \sqrt{\sum_k \delta_k^2} \quad (5)$$

Thus, the uncertainty in the $\Delta\Delta G^\circ$ described above and characterized by N_A independent simulations of $\Delta G^\circ(A)$ and N_B independent simulations of $\Delta G^\circ(B)$ is given by

$$\delta(\Delta\Delta G^\circ(A, B)) = \left(\frac{1}{N_A} \sum_{i=1}^{N_A} (\Delta G_i^\circ(A) - \Delta G_{\text{pooled}}^\circ(A))^2 + \frac{1}{N_B} \sum_{j=1}^{N_B} (\Delta G_j^\circ(B) - \Delta G_{\text{pooled}}^\circ(B))^2 \right)^{\frac{1}{2}} \quad (6)$$

Assessment of Convergence. Trajectory Truncation. To estimate the equilibration time, we excluded increasing portions of each window trajectory from its beginning. As this equilibration time is extended, the sampling is more distant from the system-building procedure and thus less perturbed by it. We truncated between 0 and 600 ns from each trajectory, in steps of 100 ns. We then used these FECs to calculate a series of $\Delta G_{\text{stretch}}^\circ$.

In a second analysis, the trajectories were truncated from the end, again in 100 ns increments and removing between 0 and 600 ns. This analysis exposes how our results would vary if we had stopped the simulations earlier.

Covariance Overlap by Window. We used a singular value decomposition (SVD) to solve for the eigenvalues and eigenvectors of the atomic motions in the simulations representing each window and then computed the covariance overlap of the eigenvectors to evaluate their similarity^{82–84}

$$\Omega_{A,B} = 1 - \left(\frac{\sum_{i=1}^{3N} (\lambda_i^A + \lambda_i^B) - \sum_{i=1}^{3N} \sum_{j=1}^{3N} \sqrt{\lambda_i^A \lambda_j^B} (\nu_i \cdot \nu_j)^2}{\sum_{i=1}^{3N} (\lambda_i^A + \lambda_i^B)} \right)^{1/2} \quad (7)$$

where $\Omega_{A,B}$ is the covariance overlap between trajectories A and B for N selected atoms, λ_i^A is the i th eigenvalue of the covariance matrix from A , and ν_i is the corresponding i th eigenvector. We used the Lightweight Object-Oriented Structure analysis library project, LOOS, to perform the SVD and to calculate the covariance overlap.^{84,85}

For each window, all heavy atoms in all four trajectories were aligned consistently.⁸³ SVDs were then computed for each replica of each window. The covariance overlap was then computed for each nonredundant pairwise combination of the four replicas. We averaged the resultant per-window scores and estimated the quality of that average by computing the SEM where the number of replicas (not the number of combinations of replicas) determined the sample size.

All-to-All RMSD of Neighboring Windows. For WHAM, sequential windows must contain overlapping probability distributions along the reaction coordinate; otherwise WHAM

will produce a discontinuous free energy curve. The theoretical basis of umbrella sampling, however, is repeated free energy perturbation; therefore, the windows must overlap in a more complete phase space.⁷¹ Overlap along our reaction coordinate is good, as evidenced by our smooth FECs. To score phase-space overlap in dimensions not well characterized by our reaction coordinate, we assessed the similarity of loop structure in consecutive windows by computing a root-mean-squared displacement between each frame (an “all-to-all” RMSD) in trajectories from neighboring windows for all heavy atoms in the loop (residues 3–9). We wrote a LOOS tool called rms-overlap to perform the calculations between frames from two user-specified sets of trajectories, and we included it with the tools distributed with LOOS.^{85,86}

To score similarity between windows, we considered a fraction of frame pairs whose RMSD was below a chosen cutoff (2.5 Å). An RMSD between loop heavy atoms below this cutoff implies similar conformations. This quantity could be computed for any two windows or, indeed, any pair of trajectories. We refer to the fraction, F , for two windows (named by their window indices) v and w , as $F(v, w)$. Because we were interested in scoring overlap along the reaction coordinate, we only considered neighboring windows, $F(w, w+1)$. We also computed a ratio of the neighboring fraction of frame pairs below the cutoff to the average fraction of frame pairs within the two neighboring windows that are below the cutoff

$$R(w, w+1) = \frac{F(w, w+1)}{\frac{1}{2}(F(w, w) + F(w+1, w+1))} \quad (8)$$

This ratio is a clearer representation of the degree of overlap where $F(w, w+1)$ is small (less than 0.1) because $F(w, w)$ and $F(w+1, w+1)$ are also small. This occurs when windows with high conformational heterogeneity are compared. We used pooled frames from all four trajectories of each window sampled every 500 ps to compute these values.

FEC Numerical Derivatives. To evaluate which bins along the reaction coordinate exhibit greater variation in free energy, we computed a numerical derivative of the FEC using the “gradient” method provided by the NumPy software package for Python.^{87,88} We then computed the standard deviation of this quantity, σ , across the four replica distributions of each bin, with the mean as the free energy resultant from the pooled distributions.

To quantify these values per window, we collected the FEC derivative curves into segments where the center of the segment was the restrained distance of the associated window. We assumed that each segment should be 1 Å wide, in keeping with our restraint spacing (except for the first and last windows, which we only made 0.5 Å wide to avoid edge effects). We integrated the derivatives over these segments using Simpson’s rule as implemented in SciPy and then computed the σ of each segment.⁸⁹ This quantity is in units of energy, and computing its standard deviation provides a score of the variability observed within a window. We provide the Python script that we used to perform these calculations on FEC data files as [Supporting Information](#) and on GitHub (<https://github.com/lgsmith/derivative-stats>). This method is general to any comparison between curves with arbitrary zeros, where the same problem (of offsets in parts of the curve proximal to the zero rendering a variance distal to the zero incoherent) would apply for repeated measurements of the same curve.

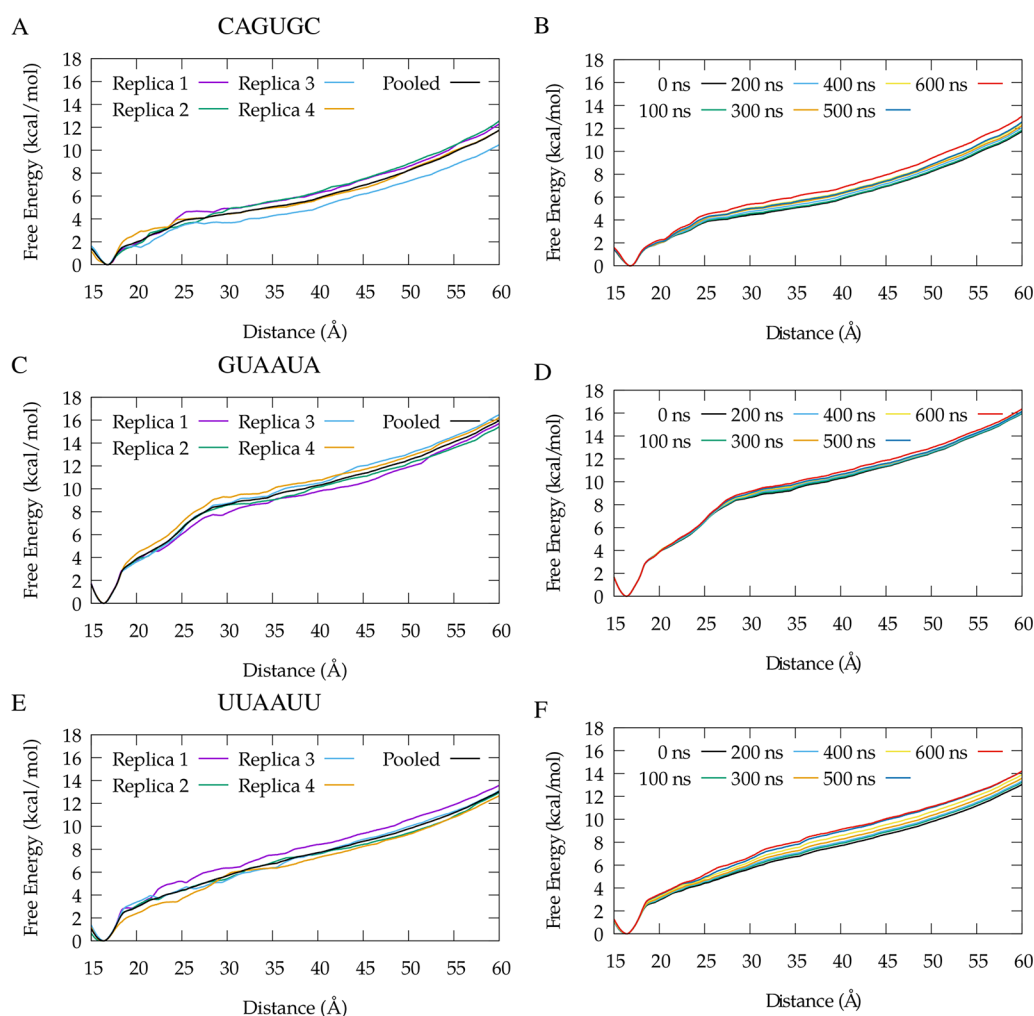


Figure 3. FECs. (A,C,E) Four replicas of the equilibrium-excluded data for each system plus the FEC produced by pooling that data, which is our best estimate for the FEC. (B,D,F) Results of the pooled data from trajectories with data excluded from their ends in 100 ns increments. Panels (A) and (B) correspond to CAGUGC, (C) and (D) correspond to GUAAUA, and (E) and (F) correspond to UUAAUU. For each truncated FEC, the curve corresponding to “0 ns excluded” is the same as the pooled data in the plots showing the overlay of the replicas of each system. Note that all FECs are zeroed at their minimum value, which happens to be the same (the location of the native state, 17 Å) for all 12 FECs.

RESULTS

Free Energy Curves. We obtained free energy curves for the three sequences (Figure 1) using WHAM as applied to our umbrella sampling simulations (Figure 3A,C,E). Our best estimate for the FECs excludes the first 200 ns of sampling for equilibration and pool the sampling from each replica of each window before running WHAM. This best estimate is shown in black and is considered the full length data set. Because the simulations were done in quadruplicate, overlaying the FECs shows regions that disagree across replicas. While agreement does not guarantee convergence, disagreement is necessarily the result of insufficient sampling, though not always in the same bin as the disagreement (see the section below on [Per-Bin Free Energy Variation](#)). Thus, it appears that our simulations provide consistent representations of the native basin, the region surrounding the native structure at approximately 17 Å, and of the extended structures present beyond 45 Å. This is unsurprising; these regions of the reaction coordinate should correspond to relatively small volumes in phase space by comparison with the middle of the reaction coordinate, where the native stem is lost but the backbone is not taut.

To assess convergence, we removed increasingly large sections from the end of the trajectory of each replica in 100 ns increments before pooling them and applying WHAM, as before (Figure 3B,D,F). This addresses the extent to which the “best estimate” provided by the pooled data is sensitive to the length of the simulations. We note that these curves exhibit some disagreement when they are zeroed at their minima, 17 Å. We quantify the extent to which this disagreement affects the calculation of ΔG° values from these data in the section below on [Free Energy Changes](#).

Hydrogen Bonding and Reaction Coordinate Partitioning. To identify the boundary between the native basin and the denatured state, we computed the average occupancy of hydrogen bonds between non-neighboring bases along the reaction coordinate. We found that this average consistently drops to 0.3 hydrogen bonds or below at 45 Å and, with the exception of the 53 Å window from the first replica of CAGUGC, remains near 0 along the rest of the reaction coordinate (Figure 4A). By monitoring all hydrogen bonds, we considered non-native structures forming in windows that are near the native basin but distant enough to have disrupted the helix as nonstretched structures. This can be seen from the

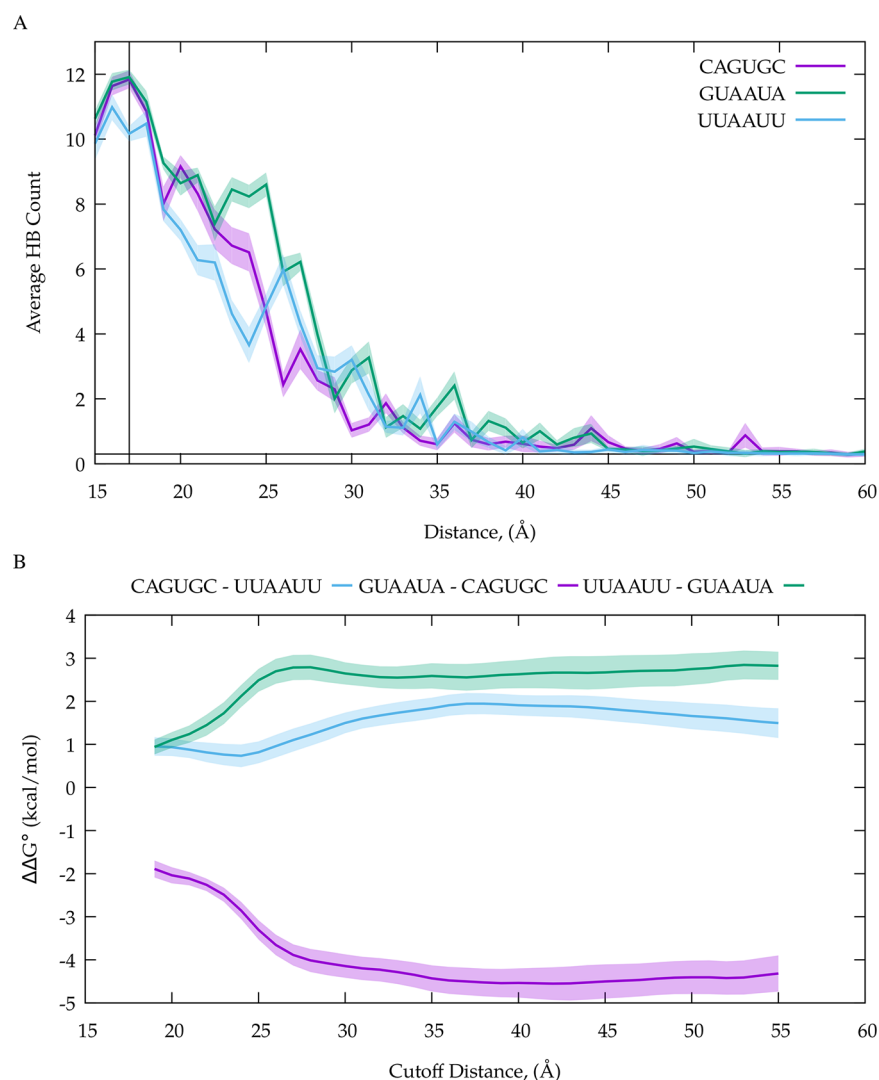


Figure 4. Estimation of the cutoff between the slack and stretched states. (A) Average occupancy of non-neighboring base–base hydrogen bonds as a function of end-to-end distance. The transparent envelopes represent the SEM. The hydrogen bonds were defined by an angle cutoff of 30° and a heavy atom distance cutoff of 3.5 \AA . The horizontal line is at 0.3 average hydrogen bonds. The vertical line at 17 \AA indicates the end-to-end distance of the native Watson–Crick helix. (B) $\Delta\Delta G^\circ$ (eq 2) for a pair of sequences as a function of cutoff distance (eq 1). The envelopes show the SEM.

heterogeneity in the hydrogen bond plots across sequences. In addition, there is also variability across replicas. The most consistent pattern is the near absence of such hydrogen bonds beyond 45 \AA , and we therefore chose this as the boundary between slack and stretched. To further support our choice, we plotted the $\Delta\Delta G^\circ_{\text{stretch}}$ as a function of boundary location (Figure 4B). By this analysis, any cutoff with distance longer than approximately 35 \AA would give results similar to those at 45 \AA . While the boundary would move for hairpin sequences of different lengths, this heuristic could still be used to identify a boundary for such systems.

Convergence and Overlap of Windows. Figure 5 shows the controls that we performed to further assess convergence and window overlap. We computed the covariance overlap (eq 7) for each replica of each window and report an average of these with an SEM as an envelope around each point in panel A. The covariance overlap gives a normalized distance between two covariance matrices. A covariance overlap of 1 would indicate that the covariance matrices are identical, whereas a covariance overlap of 0 would indicate that there is no similarity between the two covariance matrices.⁸² Because the key component of

this distance is the dot product of all pairs of eigenvectors from the covariance matrices for the two simulations (the principal components of the motions), these scores can also be viewed as measuring the extent to which the principal components overlap.^{84,90} For perspective, we computed the covariance overlap across replicas for an alignment and PCA on the helical residues of the native window. We view this as a best-case covariance overlap for structured RNA because the ends of the helix are restrained to be at the native distance and the helix should be less flexible than the loop, although the loop-closing bases and the helix-closing bases can still fray. The average and standard deviation of these calculations was 0.55 ± 0.19 . We conclude from this that there is still heterogeneity in the loop motions in restraint distances shorter than 45 \AA . However, by comparison with our helical reference, few of our windows exhibit disparate motions, and our more extended windows exhibit remarkably similar ones. We also calculated the subspace overlap of the first 25 modes of the neighboring simulations (see Supporting Information Figure 1); they were uniformly higher than the covariance overlaps, which is not surprising because the subspace overlap treats the eigenvectors as unit vectors.

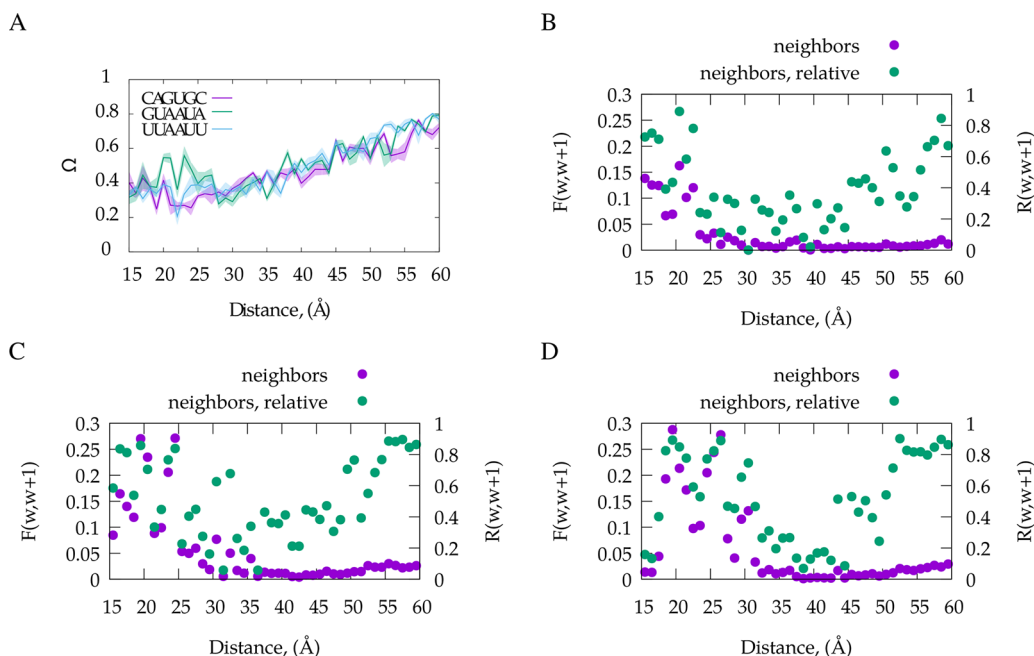


Figure 5. Assessment of convergence and phase space overlap. (A) Covariance overlap between the pooled trajectories for all heavy atoms in the loop. The bold line indicates the average value, with the transparent envelope indicating the SEM (B–D) Plots of the fraction of pairs of frames, corresponding to CAGUGC, GUAAUA, and UUAUU, respectively, with a pairwise all-heavy-atom loop RMSD less than 2.5 Å that occurs between each window w and its neighbor $w + 1$, $F(w, w+1)$ shown on the left axis. The relative fraction, $R(w, w+1) = F(w, w+1) / \frac{F(w, w) + F(w+1, w+1)}{2}$, is shown on the right axis.

To assess phase space overlap between windows, we computed the fraction of all frame pairs in neighboring windows with a loop heavy atom RMSD below 2.5 Å (Figure 5B–D). All three molecules have substantial fractions of such frames from neighboring windows before 25 Å. After 30 Å, the fraction drops below 0.05. Beyond this point, there is no native structure and most conformations are only observed for a single frame. To calibrate this fraction, we also computed a ratio between the fractions of frames below the cutoff from neighboring windows and the mean fraction across the two neighboring windows compared to themselves (eq 8). It scores overlap relative to the heterogeneity of the window under consideration, which is useful in understanding the region of low overlap in the middle of the reaction coordinate. These quantities are computed between neighboring windows. For each window, the trajectory analyzed was the pooled frames from all four of the replicas, sampled every 500 ps. Interestingly, while both scores are below 0.01 for the middle windows, for the higher windows near the “stretched” state, they begin to rise again, suggesting that those windows have more similar conformational ensembles.

Per-Bin Free Energy Variation. In the free energy curves in Figure 3, we noted a pattern in the disagreements between curves from the same sequence. Disagreement occurs starting at a certain position on the curve; the distance between a truncation and its neighbors (or a replica and its neighbors) rises and then begins to mirror its neighbors again. Because variability at a certain bin produces an offset in bins more distant from where curves are zeroed across replicas, we used a numerical derivative to identify variability between two neighboring bins (see the Methods subsection **FEC Numerical Derivatives**).

In Figure 6, the regions of lowest variability are near the native distance where the replicas are overlapped in the FEC (Figure 3). There is a region of low variability in the windows that also

lack non-neighboring base–base hydrogen bonds (Figure 4). Bins from the “stretched” state tend to be less variable than those in the extended but not the taut middle region of the curve. The variability in CAGUGC corresponds to rearrangement in the base pairing of the terminal base pair in shorter than native distance (compressed) windows in some replicas.

The window integrals of the standard deviation (Figure 6B–D) suggest the extent of convergence for individual windows with respect to their part of the FEC. Low-variability windows have almost no (less than 0.1 kcal/mol) difference between the truncated and full trajectories, and the total variability estimated from truncations also remains low (below 0.15 kcal/mol). Windows that vary substantially can be twice as variable for truncated trajectories and even with a full data set score higher than 0.2 kcal/mol.

Free Energy Changes. To estimate how much of the trajectory to exclude as equilibration, we plotted the free energy of stretching (eq 1) from end-distance distributions that had been truncated from the beginning in 100 ns increments in Figure 7A. While it is challenging to determine how much equilibration is sufficient and not excessive, for two of our three systems it appears that the free energy of stretching stops systematically changing after the first 200 ns. For UUAUU, there appears to be a steadier drift in the value of free energy that occurs over the course of the trajectories, although it leveled off considerably after excluding 200 ns. On the basis of this evidence and by inspecting our FEC derivatives as a function of truncation from the beginning, we conclude that a 200 ns equilibration is sufficient. With the equilibration period removed, Figure 7B shows that truncating from the end of the trajectories does not substantially change the free energy of stretching. For example, removing 200 ns of sampling from the end changes the folding free energy by less than 0.5 kcal/mol. This demonstrates the degree of convergence that is achieved with the sampling. We

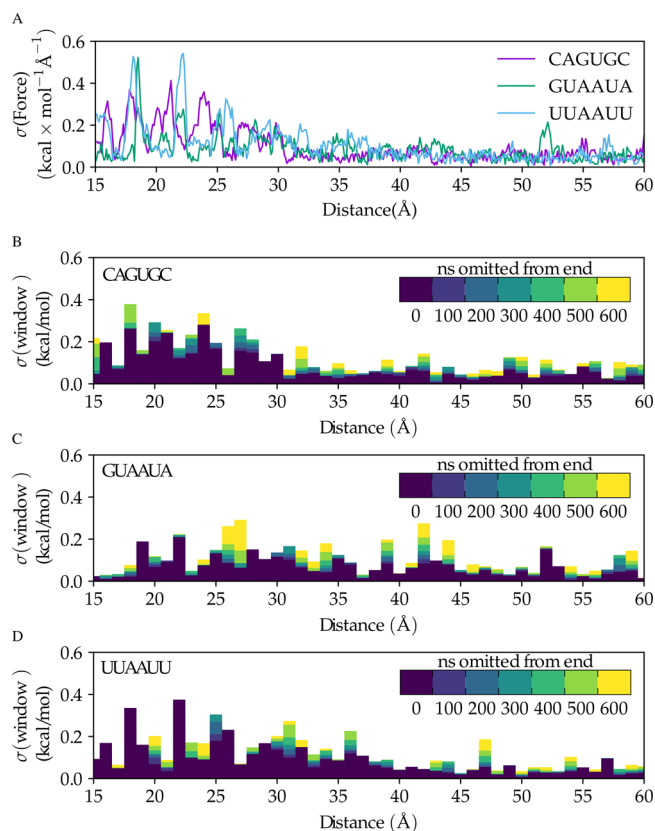


Figure 6. Standard deviation, σ , per bin in the FECs. (A) σ for the derivative of each FEC with respect to the reaction coordinate (see Methods subsection [FEC Numerical Derivatives](#)) for data derived from the full length trajectories. (B–D) Regions corresponding to each window integrated along the reaction coordinate using the Simpson's rule and plotted as boxes. The longer trajectories (fewer ns omitted from the end) are overlaid on the shorter trajectories.

note that UUAUU is the least well converged of the three sequences.

To compare our stretching experiments to experimental folding stabilities ([Tables 1 and 2](#)), we followed the approach from Spasic et al.,⁵³ where a thermodynamic cycle describing differences in folding stability ([Figure 2](#)) was used. By approximating the stretched to random-coil transition as sequence-independent, we can compare the $\Delta\Delta G^\circ$ between two sequences to analogous differences in stability from optical melting experiments. The sequence independence assumption was used previously to compare the free energy changes of single-molecule pulling experiments to optical melting experiments.⁵⁹ In those studies, a polymer theory model was used to estimate the entropic difference between the random coil and the stretched state, and good agreement between the two experimental methods was shown. Here, we use a more conservative assumption by using the thermodynamic cycles to account for the entropic cost rather than using a model to estimate the cost.

To quantify the sequence independence of the stretched state from our data, we fit the free energy curves to quadratic functions in the stretched region (45–60 \AA) and found that the quadratic and linear coefficients are similar ([Supporting Information Table 2](#)). Further, if the curvature of the FECs were different in the more stretched region, our $\Delta\Delta G^\circ_{\text{stretch}}$ would be sensitive to cutoff choice (see [Figure 4B](#)). This lack of variability in the stretched region of the curve supports our

approximating it as sequence-independent; if the curve were variable in this region, it would be harder to distinguish whether this variability were a property of the sequence or whether it was random variability from sampling.

[Table 1](#) shows the changes in ΔG° that we observed. As discussed in the [Introduction](#), the changes in state between the in silico stretching and in vitro optical melting are not the same; therefore, it is expected that these free energies would be different. Our assumption that the differences in stabilities between sequences ([Table 2](#)) should be comparable whether the stabilities were obtained from optical melting experiments or our free energy estimates by stretching also implies that there is a component of the stretching free energy that is a sequence-independent offset. When we compute relative stabilities using our thermodynamic cycle, the sequence-independent components cancel. In the column of [Table 1](#) labeled " $\Delta\Delta G^\circ_{\text{melt-stretch}}$ ", we estimate this quantity by taking the difference between $\Delta G^\circ_{\text{melt}}$ and $\Delta G^\circ_{\text{stretch}}$ for the same sequence. In principle, if there were no sequence dependence and no sampling error, these numbers would be the same for all three sequences. We assessed statistical errors in our study using technical replicas; therefore, differences in this quantity that are outside of our uncertainties can be interpreted as systematic differences. We estimate the difference ([Table 2](#); melt–stretch) to be similar for UUAUU and CAGUGC, but the difference for GUAAUA appears to be the outlier. It is interesting that for a similar comparison between stabilities estimated using the nearest-neighbor model²¹ and those obtained from optical melting experiments ([Table 2](#); stretch–NN), the largest outlier is CAGUGC. Our simulations appear to model the instability of this loop, although the nearest neighbor model does not.

Because the absolute value of the residuals ([Table 2](#); melt–stretch) average to 1 kcal/mol and the errors for individual residuals are of order $k_B T$, we conclude that we are nearing chemical accuracy and precision, respectively, with this technique. We propagated uncertainty in both the physical measurements and the experiments to residuals for each pair to determine whether these values are significantly different. If they were not, the residuals ([Table 2](#); melt–stretch) would be close to zero in free energy, and zero would be within the error envelope of the values. On the basis of [Table 2](#) and [Figure 8](#), we cannot reject the null hypothesis that the residuals are zero for two of the three residuals. This is also true even in highly truncated trajectories ([Figure 8](#)), and this indicates that less sampling would have reached the same conclusion. The deviation from zero residual seems to vary by sequence—the two residuals involving GUAAUA are more erroneous. While this can likely be explained in part as systematic (rather than sampling) error in these free energy differences, the differences from zero are not significant ([Table 2](#)).

DISCUSSION

FF99+bsc0+ χ_{OL3} Brackets the Relative Stability of RNA Hairpins. This study was designed to determine whether there is systematic error in the free energies simulated for RNA hairpin pulling. There is a growing consensus that the fixed charge RNA force fields for MD are inadequate, but this is commonly evaluated in a structural context with the observation that simulations do not preserve native conformations.^{25,32} However, the folding stability could be approximately correct if the number of microstates available to the RNA and their relative energies were approximately correct. Our results suggest that FF99+bsc0+ χ_{OL3} can perform with chemical accuracy to

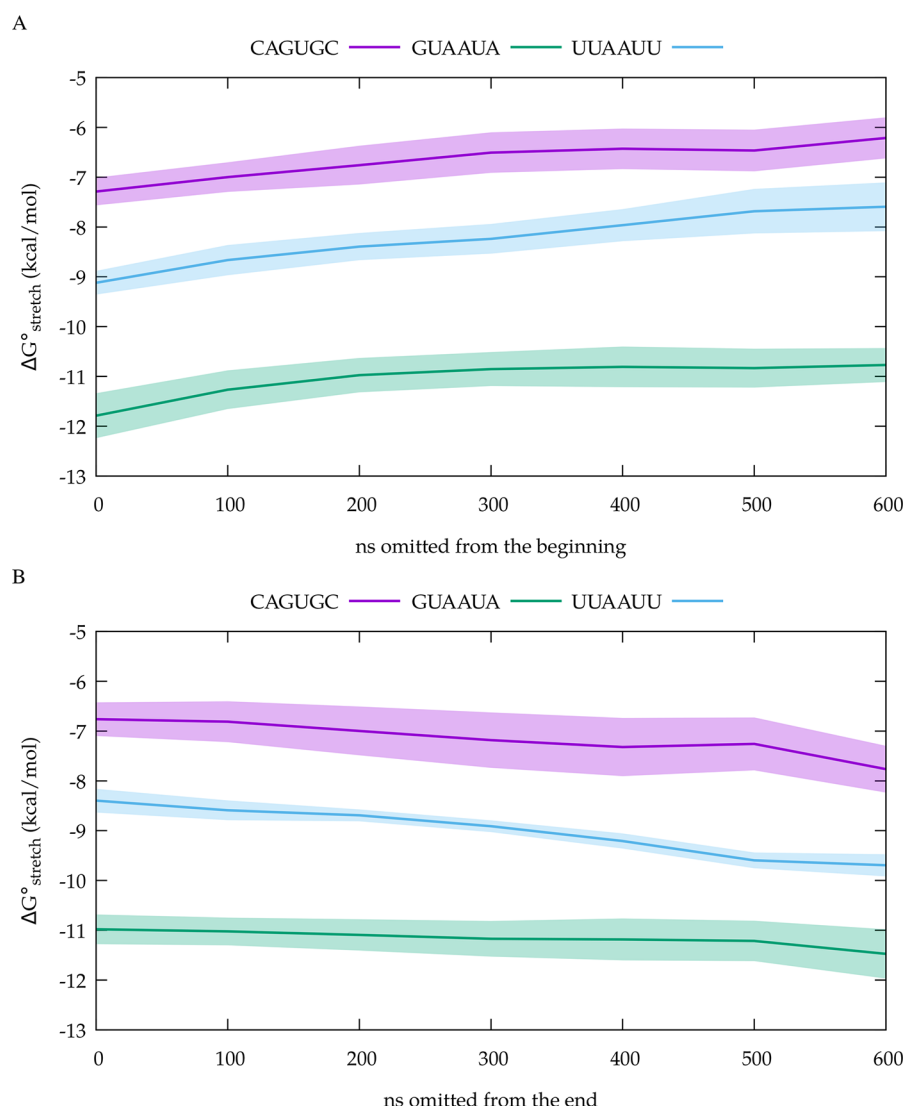


Figure 7. $\Delta G^\circ_{\text{stretch}}$ as a function of truncation. The magenta line and envelope correspond to CAGUGC, the blue to UUAUUU, and the green to GUAAUA. The lines correspond to the FEC resulting from the pooled data truncated by the amount on the independent axis. The envelope is the SEM of the pooled data with the truncated replicas treated as independent samples. (A) Relaxation of $\Delta G^\circ_{\text{stretch}}$ from the complete data set truncated from the beginning. (B) How the same quantity varies as a function of data excluded from the end of the full-length (equilibration excluded) data.

Table 1. Free Energy Changes (kcal/mol), Measured by Optical Melting, Predicted Using the Nearest-Neighbor (NN) Parameters,^{62,70} and Simulated by Stretching, for Each Sequence with Uncertainty for Each Value^a

sequence	$\Delta G^\circ_{\text{melt}}$	$\Delta G^\circ_{\text{NN}}$	$\Delta G^\circ_{\text{stretch}}$	$\Delta\Delta G^\circ_{\text{melt-stretch}}$
CAGUGC	-0.21 ± 0.39	-1.61 ± 0.23	-6.75 ± 0.39	6.55 ± 0.55
GUAAUA	-3.47 ± 0.24	-3.70 ± 0.27	-10.97 ± 0.34	7.51 ± 0.38
UUAUUU	-2.35 ± 0.32	-2.05 ± 0.24	-8.39 ± 0.27	6.03 ± 0.42

^aThe variability in $\Delta\Delta G^\circ_{\text{melt-stretch}}$ quantifies the error in the thermodynamic cycle calculations because that quantity should be a constant up to the variability from incomplete sampling. The mean with propagated error for this quantity is 6.70 ± 0.79 kcal/mol.

estimate relative stabilities of RNA hairpins along an end-to-end reaction coordinate with adequate sampling. Despite the known problems with force fields, the relative folding free energies of RNA hexaloops can be adequately modeled with FF99+bsc0+ χ_{OL3} .^{25,32,33,37}

This work also provides a framework for benchmarking force fields that display incremental progress, which is a current challenge. Consider, for example, comparisons between simulations and two-dimensional Nuclear Overhauser Effect (NOE) spectra.²⁵ It is clear that a simulation indicating the

presence of strong NOE cross-peaks that are not observed in experimental spectra of the same system is a problem. What is not clear is how inaccurate this comparison shows the force field to be. It is conceivable that minor adjustments in the right parameters would tune the force fields and eliminate these artifacts entirely, although we find this unlikely given the breadth of efforts, including our own, to rectify these issues.⁴⁰ Such efforts have, in some cases, resulted in force fields that sample structures with unobserved NOEs less frequently but do not totally reduce them to levels that would be undetectable by

Table 2. Difference in Free Energy Change (kcal/mol) of Unfolding for Pairs of Sequences^a

reactant	product	$\Delta\Delta G_{\text{stretch}}^{\circ}$	$\Delta\Delta G_{\text{melt}}^{\circ}$	$\Delta\Delta G_{\text{NN}}^{\circ}$	melt–stretch (<i>P</i>)	stretch–NN (<i>P</i>)
GUAAUA	UUAUUU	2.58 ± 0.44	1.11 ± 0.40	1.65 ± 0.35	$1.47 \pm 0.60(0.90)$	$0.93 \pm 0.57(0.198)$
UUAUUU	CAGUGC	1.64 ± 0.48	2.15 ± 0.52	0.44 ± 0.33	$-0.52 \pm 0.70(0.514)$	$1.20 \pm 0.58(0.131)$
CAGUGC	GUAAUA	-4.22 ± 0.52	-3.26 ± 0.46	-2.09 ± 0.36	$-0.95 \pm 0.70(0.264)$	$-2.13 \pm 0.63(0.044)$

^aEach of these differences is from the thermodynamic cycle in Figure 2. The differences are calculated as alchemical transitions between sequences, with $\Delta\Delta G^{\circ} = \Delta G_{\text{product}}^{\circ} - \Delta G_{\text{reactant}}^{\circ}$. The “stretch” transitions are those estimated from simulations, and optical melting experiments are our reference data from the literature. $\Delta\Delta G_{\text{NN}}^{\circ}$ is what the nearest-neighbor model estimates for each sequence pair. The column melt–stretch is the difference between the experiment and the simulation, referred to as the residual. Stretch–NN is the difference between $\Delta\Delta G_{\text{NN}}^{\circ}$ and $\Delta\Delta G_{\text{stretch}}^{\circ}$, which shows the agreement between the nearest-neighbor model and experiment. The uncertainties given for the residuals are the uncertainties propagated from $\Delta\Delta G^{\circ}$ using eq 5. The *P* values are provided in parentheses after the residuals and are the probability of the null hypothesis that the differences are zero given the data. They are computed from a two-tailed t-test against a particular value, zero, with three degrees of freedom.

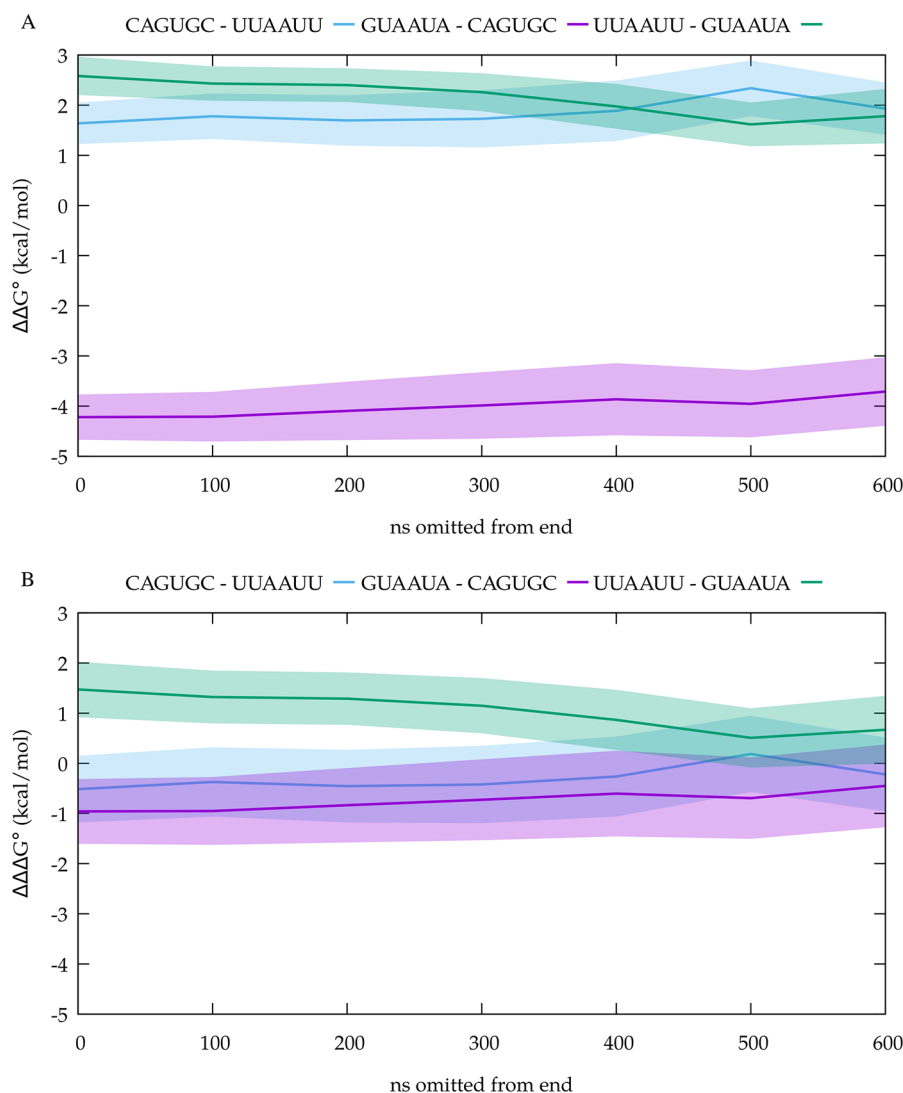


Figure 8. $\Delta\Delta G_{\text{stretch}}^{\circ}$ and residuals as a function of truncation. (A) $\Delta\Delta G_{\text{stretch}}^{\circ}$ with SEM from replicas. (B) Residual between that value and its reference $\Delta\Delta G^{\circ}$ with propagated error.

NMR. If the difference in free energy between a minor conformation and a major one is misestimated by the force field by as little as 2.0 kcal/mol at 277 K, it could be the dominant conformation in the simulation and so rare in reality as to be unmeasurable by NMR. Because we cannot measure the features of the free energy surface of the tetramer systems experimentally, it is challenging to differentiate between force fields that are becoming more accurate from those that are introducing new errors. In particular, it is hard to determine

whether a given modification is part of a necessary set of changes to the force field but not in its own right sufficient. The progressive nature of free energy benchmarks therefore makes them a needed addition to the force field test suite.

Convergence. In principle, MD allows sampling of the thermodynamic ensemble of the simulated system. This ensemble could then determine any equilibrium quantity of interest and be compared with or estimate experimental data. In practice, especially because of technological limits, sampling is

usually incomplete, causing statistical errors.²⁴ For RNA simulations, the statistical problem is pronounced; while protein folding simulations have been the focus of pioneering work in enhanced sampling,⁹² for swarms-of-trajectories approaches that harness the aggregate idle power of many personal computers⁹³ and, most recently, brute force sampling by specialized supercomputers,⁹⁴ similar simulations of RNA have either only been tried recently³² or have not yet been performed. Because of this lack of focus by the broader MD field, the source of reported inaccuracies is not obvious.

The RNA folding landscape is not completely defined by the end-to-end distance. For specific windows in umbrella sampling, there might be slowly equilibrating degrees of freedom that are nearly orthogonal to the reaction coordinate, and some of these degrees of freedom might be poorly sampled. These degrees of freedom must overlap for the results of an umbrella sampling approach to be interpretable, even though the overlap between adjacent windows along the reaction coordinate determines whether WHAM produces a continuous curve. To score the overlap of window ensembles on potentially orthogonal degrees of freedom, we considered all-to-all frame RMSDs for neighboring windows along the reaction coordinate (Figure 5B–D). This RMSD was calculated for all heavy atoms in the loop residues. The loop is the most distal part of the RNA from the restraint and, therefore, the most likely to contain degrees of freedom for which the biasing potentials enhance sampling the least.

In the longer distance windows, the restraint becomes a more effective bias for all of the degrees of freedom (Figure 5). Within more distal windows (those above a 25 Å restraint distance), there is still conformational heterogeneity, as evidenced by the relatively low fraction of frame pairs below our cutoff; however, it appears that these windows exhibit less diverse motion according to the covariance overlap, suggesting that perhaps lever-arm effects from the extended structures are at play in reducing the fraction of frame pairs below the RMSD cutoff.

While the relative fraction of pairwise RMSDs suggests that there is less overlap of ensembles in the middle windows, we note that no neighboring windows have zero frame pairs below the 2.5 Å cutoff in RMSDs. We also note that this calculation, where only the loop conformations are scored, is a conservative choice. If we had selected all heavy atoms, the molecule overlaps would have been higher because they would have contributions from atoms that are more directly restrained to be in similar positions. Finally, we note that, in studying the variation in FEC derivatives per window (Figure 6), it appears that windows for distances of 26–60 Å (the windows with the greatest conformational heterogeneity by this metric) result in the smallest changes in the free energy curves themselves. Their loop motions are also more self-similar (Figure 5A), even though the loop structures are not self-similar (Figure 5B–D). In other words, for the purposes of precisely calculating the free energy of stretching, additional sampling of the middle and terminal windows would yield the least change in the computed free energies. It therefore appears that our reaction coordinate is nearly orthogonal to the loop conformations in the midrange windows.

One might wonder whether, with more extensive sampling, we might find our residuals trending to zero. While this question is hard to answer, considering the residual as a function of truncation might suggest whether extending our sampling further would result in different conclusions.⁹⁵ From Figure 8, we see that the residuals increase as the trajectory gets shorter,

which is what one might expect if instead of excluding unequilibrated parts of the trajectory we were simply excluding viable samples from our data set.

Reaction Coordinate. The major benefit of the end-to-end distance reaction coordinate is the well-defined character of the end point. Sampling the random coil ensemble for RNA large enough to have structure is not feasible given the level of access that most simulators have to computing power. Thus, simulations of stretching transitions are more likely to provide useful estimates of stability given current technology. A minor benefit is that force-driven extension experiments also follow this reaction coordinate, although the single-molecule experiments currently require structures that are too large to be able to sample adequately on current hardware.

Simulations estimating stability from pulling-like restraining forces have historically suffered from the problem of having more arbitrary distinctions between native and stretched states.^{38,96} Using the aggregate non-neighboring base–base hydrogen bonds as a score of extension avoids the problem of searching for a point along the reaction coordinate where native structure has been lost. This point is not always obvious because it is difficult to distinguish between native fluctuations and an unfolded conformation. Our choice is a way to define the point where the chain is stretched, which allows us to lump many of these potentially native-like structures into the slack state. The hydrogen bond metric can be applied to unimolecular stretching experiments of RNAs of arbitrary size and sequence. Critically, using thermodynamic cycles to consider $\Delta\Delta G_{\text{stretch}}^{\circ}$ for the purposes of comparison avoids much sensitivity to the choice of this boundary, and our boundary choice resides in the middle of the plateau in the sensitivity plot of these quantities (Figure 4B).

Standard Deviation of the Free Energy Derivative. In umbrella sampling, a deviation between two technical replicas is usually particular to specific bins along the reaction coordinate. It is problematic to characterize the deviation using a standard deviation per bin because the bins are zeroed at one arbitrary location along the reaction coordinate. At points along the reaction coordinate distant from the zeroed location, statistical fluctuations will have accumulated. Computing a variance or standard deviation with these values directly would therefore be incorrect.

To assess the agreement in FECs locally, we computed the standard deviation in the numerical derivative of the FEC across replicas (see the subsection **FEC Numerical Derivatives** in the Methods section and Figure 6). We submit this as the best approach for analyzing FECs as it provides information about consistency and accurately identifies regions of disagreement across replicas or even across subdata sets. It would certainly apply to discretized FECs assembled from simulations by other means, such as the Multistate Bennett Acceptance Ratio,⁹⁷ weighted ensemble simulation,⁹⁸ and well-tempered Metadynamics.⁹⁹ Computing numerical integrals of this quantity across the width of a window illustrates how variability is localized to a given window. Both quantities combine nicely with data set exclusion approaches such as those discussed in the subsection **Trajectory Truncation** because they can indicate which parts of a FEC are not as well converged.

Thus, both quantities would find use in further efforts to converge umbrella sampling calculations. The window integral standard deviations indicate windows that need further sampling. To initialize simulations for additional sampling, the derivative can suggest what frames to start from because it is a per-bin score of variability. Frames from a variable window

exhibiting distances along the reaction coordinate that would be binned under a peak in the derivative curve are the best frames from which to start new simulations because they are adjacent to some undersampled event that has resulted in variability at that position. This could be done to adaptively guide additional sampling while simulations are ongoing.

Furthering In Silico Pulling. A number of approaches could be used to improve the efficiency of these types of in silico pulling experiments. Our results specifically suggest the following:

1. Sample the stretched state less or not at all. The stretched windows do not contain much information about our systems but are the most computationally expensive because they are larger and therefore have much greater water content. The windows with restraint distances of 45 Å and greater are some of the most well converged by our metrics, especially the covariance overlap and the free energy derivative SDs. Because we approximate the stretched state as sequence-independent, we could add additional sequences to our analysis by averaging the stretched windows together and considering only their differences in the slack state or by simply subtracting their slack-state sums from one another.
2. Use pioneer simulations to compute $\Delta\Delta G_{\text{stretch}}^{\circ}$ with a range of state boundaries (as in Figure 4B) to determine how far to stretch and where to position the state boundary. As above, this would reduce the amount of uninformative stretched windows being simulated. It is also a needed control for thermodynamic cycle analysis because the $\Delta\Delta G_{\text{stretch}}^{\circ}$ will become constant at some boundary when the FECs are converged.
3. Sample the native basin less. Although these windows are not as expensive to run, they also show so little variability across both replicas and slices that having run them for much less time (a factor of 10 less) would not have perturbed the free energy change estimates.
4. Extend the sampling for windows that show deviation across slices. By the same logic as the previous three points, windows that show high variability are necessarily more poorly defined and will therefore change the resultant free energy change of stretching the most if more completely sampled. Use the standard deviation of the FEC derivative approach to identify which regions produce this variability and to determine the starting structures for follow-up simulations that would target them.
5. Use window-to-window Hamiltonian replica exchange. Using replica exchange to exchange restraints between neighboring windows is a classic technique in umbrella sampling simulations that enhances convergence across the FEC.⁴⁴ While our computational environment restricted us from using this technique on all windows, identifying poorly behaving windows given sequence length (for us the range is consistently 18–25 Å) may markedly speed up convergence in these regions.
6. Bias other reaction coordinates to more efficiently sample the loss of structure. End-to-end distance may not be the most efficient path between the native structure and a stretched state. Because such simulations possess both well-defined start and end points, path-finding methods like nudged elastic band^{100–102} or finite temperature string methods^{103–106} might provide more useful window

spacings, window positions, or additional restraints. Such methods might yield reaction coordinates that, while specific to RNA (and likely to RNA of a particular length), are not particular to any sequence, allowing results from a few careful reaction coordinate-finding simulations to be used for many new RNA sequences.

7. Use fixed positional restraints rather than distance restraints. This would eliminate RNA's translational and rotational degrees of freedom, and restraining the end-to-end positions of the RNA would then allow a hexagonal prism or rectangular box to be used, which would reduce the number of solvent molecules in more extended windows. This also mimics stretching experiments more directly because having both ends of the chain tethered prevents long axis rotations and, for a given extension distance, center of mass translations.
8. Analyze error by computing the average difference between RNA stretches and melts (Table 1). This value can be thought of as the sequence-independent free energy of relaxation from stretched to random coil states (and sequence-independent errors of stretching or of the force field) that is being subtracted away in the thermodynamic cycle. This error term should contain both systemic, sequence-specific error and sampling error, but the variability in it is already low enough to discern outliers (GUAAUA is more overly stable than the other two sequences). Adding to the diversity of stretched sequences would make such an observation a more firm conclusion. It would also allow the approximate accuracy of a newly stretched sequence to be estimated without multiple replicas or reference to a pre-existing melt, which will be important in the future as this technique becomes more accurate and the collection of sequences with known reference melts to which it has been applied grows.

CONCLUSIONS

In this study, we furthered an approach to compare in vitro folding stabilities and in silico free energy curves. We refined methods for analyzing such data and situated future studies on this topic to add sequence diversity more efficiently. Most notably, we showed that the thermodynamic landscape of FF99+bsc0+ χ_{OL3} is chemically accurate where previously questions had lingered about whether differences could be due in part to lack of convergence.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jctc.8b00633.

Tables of fit constants to curve segments (PDF)

Scripts for analyzing free energy, free energy variance, and our raw distance files (ZIP)

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Notes

The authors declare no competing financial interest.

The Python script that we used to perform these calculations on FEC data files is available on GitHub <https://github.com/lgsmith/derivative-stats>.

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